

Answer Keys

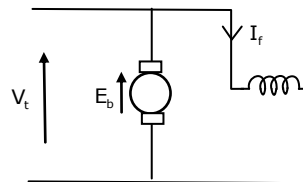
1	D	2	B	3	A	4	D	5	A	6	D	7	B
8	B	9	C	10	4	11	3.33	12	C	13	C	14	A
15	D	16	B	17	D	18	A	19	D	20	225	21	76.4
22	C	23	B	24	50	25	A	26	C	27	B	28	D
29	98.8	30	78	31	84	32	0.448	33	99.4	34	B	35	B
36	A	37	B	38	A	39	D	40	C	41	C	42	A
43	40	44	300	45	C	46	D	47	A	48	2	49	2.666
50	2500	51	7.5	52	C	53	D	54	A	55	D	56	C
57	D	58	A	59	C	60	A	61	D	62	B	63	C
64	D	65	D										

Explanations:-

1. $z = \frac{10 \angle 0}{5 \angle -30} = 2 \angle 30$; $10 \cos \omega t + 30^\circ = 10 \sin 90 - \omega t - 30^\circ = 10 \sin 60 - \omega t$
 $= -10 \sin \omega t - 60 = -10 \angle -60^\circ$, $I = \frac{V}{Z} = \frac{-10 \angle -60}{2 \angle 30} = -5 \angle -90 = 5 \angle 90$
 $= 5 \sin \omega t + 90 = 5 \cos \omega t$ A

2. $x \cdot 0 = \lim_{s \rightarrow \infty} s \times \frac{3 + \frac{4}{s}}{\frac{1}{s} + 1} = \lim_{s \rightarrow \infty} \frac{3 + \frac{4}{s}}{\frac{1}{s} + 1} \cdot s = 0$

4. With losses neglected $V_t = E_b$
 When V_t is halved, E_b is halved.
 Now for constant power
 $E_b I_a = \text{constant}$ so I_a is doubled.
 Again, with V_t halved, I_f is halved, so is ϕ
 $E_b = \omega \phi$
 E_b and ϕ are halved, $\omega = \text{constant}$
 $T_\omega = \text{constant}$ so, T is constant



7. Since rank = 2
 $\Rightarrow |A| = 0$
 $\Rightarrow \begin{vmatrix} k & -1 & 0 \\ 0 & k & -1 \\ -1 & 0 & k \end{vmatrix} = 0 \Rightarrow k = 1$

8. we have $\int_a^b \frac{f(x)}{f(x) + f(a+b-x)} dx = \frac{b-a}{2}$

$$\therefore \int_2^4 \frac{\sqrt{x}}{\sqrt{x} + \sqrt{6-x}} dx = \frac{4-2}{2} = 1$$

9. $\frac{ds}{dt} = 32t - 2$

$$\Rightarrow ds = (32t - 2)dt$$

$$\Rightarrow \int ds = \int (32t - 2)dt$$

$$\Rightarrow s = 32 \frac{t^2}{2} - 2t + c \dots (1)$$

given $s\left(\frac{1}{2}\right) = t$

$$\Rightarrow \text{when } t = \frac{1}{2}, s = 4$$

from (1), $4 = 16\left(\frac{1}{2}\right)^2 - 2\left(\frac{1}{2}\right) + c$

$$\Rightarrow c = 1$$

$$\therefore s = 16t^2 - 2t + 1$$

10. $f_1 = 20\text{Hz}; f_2 = 30\text{Hz};$

Analog frequencies, Digital frequencies are $F_1 = \frac{20}{75} = \frac{4}{15} = \frac{K_1}{N_1}$

$$F_2 = \frac{30}{75} = \frac{2}{5} = \frac{K_2}{N_2}; \therefore N_1 = 15, N_2 = 5; K_1 = 4, K_2 = 2$$

11. $L_1 = 1\text{H}, L_2 = 2\text{H}$

$$i(0^+) = \frac{L_1}{L_1 + L_2} i(0^-) = \frac{1}{3} \times 10 = \frac{10}{3} \text{ A} = 3.33 \text{ A}$$

13. Re active power $Q = \frac{E_f V_t}{X_d} \cos \delta - \frac{V_t^2}{X_d} - V_t^2 \left(\frac{1}{x_q} - \frac{1}{x_d} \right) \sin^2 \delta$

$$V_t^2 \left(\frac{1}{x_q} - \frac{1}{x_d} \right) \sin^2 \delta \text{ is always positive, so for maximum } Q,$$

$\cos \delta$ needs to be maximum

$\sin^2 \delta$ needs to be minimum

So Q_{\max} occurs at $\delta = 0$

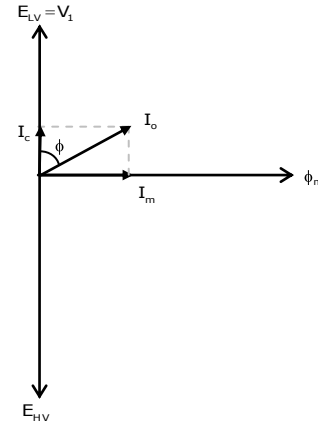
14. $I_o = 6A$

The low voltage side of transformer is excited.
So, care-loss component of no load current

$$I_c = \frac{250}{200} = 1.25A$$

$$\text{Magnetizing component } I_m = \sqrt{I_o^2 - I_c^2} = 5.87A$$

$$\text{No-load p.f.} = \cos \phi = \frac{I_c}{I_o} = 0.208$$



16.
$$y \ s = G_2 \ s \left[X \ s + x \ s \ G_1 \ s + y \ s \ G_1 \ s \right]$$

$$= \left[G_2 \ s + G_1 \ s \ G_2 \ s \right] X \ s + y \ s \ G_1 \ s \ G_2 \ s$$

$$\frac{y \ s}{X \ s} = \frac{G_2 \ s \left[1 + G_1 \ s \right]}{1 - G_1 \ s \ G_2 \ s}$$

17. The expression is simply

$$\text{Answer} = \bar{x} \pm \sigma_x$$

σ_x is the standard deviation = 0.2 sec

\bar{x} is the mean = 3.6 secs

18. $D_s = 0.7788r = 0.233 \text{ cm}$

$$\text{GMD} = D_m = \sqrt[3]{D_{ab} D_{bc} D_{ca}} = 2.29 \text{ m}$$

$$L = \frac{\mu_o}{2\pi} \ln \frac{D_m}{D_s} = 1.38 \times 10^{-6} \text{ H/m} = 1.38 \text{ mH/km}$$

$$L = 1.38 \times 10^{-3} \times 125 = 0.1725 \text{ H}$$

$$X_L = \omega L = 2 \times \pi \times f \times L = 2 \times \pi \times 50 \times 0.1725 = 54.19 \Omega$$

19. We have

$$\text{Res } f(z) = \lim_{z \rightarrow x} \left\{ \frac{1}{n-1!} \frac{d^{n-1}}{dz^{n-1}} \left[(z-a)^n f(z) \right] \right\}$$

at $z = a$

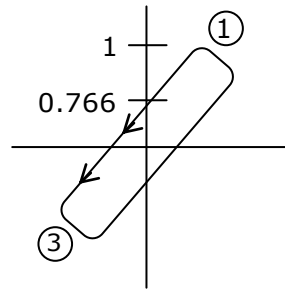
$$\Rightarrow \text{Res } f(z) \text{ at } z = -1 = \lim_{z \rightarrow -1} \left\{ \frac{1}{2-1!} \frac{d^{2-1}}{dz^{2-1}} \left[(z+1)^2 \frac{2}{(z-1)(z+1)^2} \right] \right\} = \lim_{z \rightarrow -1} \frac{d}{dz} \left(\frac{z}{z-1} \right)$$

$$\text{at } z = a = \lim_{z \rightarrow -1} \left\{ \frac{(z-1) \times (1) - z \times (1)}{(z-1)^2} \right\} = \lim_{z \rightarrow -1} \frac{z-1-z}{(-1-1)^2} = -\frac{1}{4}$$

20. Utilization factor = $\frac{\text{capacity factor}}{\text{Load factor}} = \frac{0.750}{0.65} = 0.7692$
 \therefore Plant capacity = $\frac{\text{Maximum demand}}{\text{utilization factor}} = \frac{750}{0.7692} = 975.039 \text{ MW} \approx 975 \text{ MW}$
 Reserve capacity = Plant capacity – max.demand = 975 – 750 = 225 MW
21. Number of parallel paths = 6
 \Rightarrow Number of series devices = $\frac{60}{6} = 10$
 \therefore series string efficiency = $\frac{\text{Final rating}}{\text{Number of devices} \times \text{device rating}}$
 $= \frac{10 \times 10^3}{10 \times 1.2 \times 10^3} = 0.833$
 Parallel string efficiency = $\frac{5.5}{6 \times 1} = 0.9167$
 \therefore total string efficiency = $0.833 \times 0.9167 = 0.76385$
 \therefore % efficiency = 76.4%

22. $8V = 1600I_D + V_{DS} + 400I_D$, $8 = 2000I_D + V_{DS}$; $2000I_D = 8 - V_{DS}$
 $I_D = \frac{8}{2000} - \frac{V_{DS}}{2000} = \left(\frac{-1}{2000}\right)V_{DS} + \left(\frac{8}{2000}\right)$, $\boxed{m = \frac{-1}{2000}}$; $y = I_D$; $x = V_{DS}$

24. $\phi = \sin^{-1} \left[\frac{Y_1}{Y_2} \right]$
 $= \sin^{-1} \left(\frac{0.766}{1} \right) = 50^\circ$



25. $f' = x'y'z' + x'y'z + x'yz' + x'yz + xy'z' + xy'z + xyz$

x	y	z	f'
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	1	1	1
1	0	0	0
1	1	1	1

$\therefore f = xyz'$

26. After closing the switch,

$$V_+ = Ve^{-t/\tau} = 100e^{-1000t}, V_- = V(1 - e^{-t/\tau}) = 100(1 - e^{-1000t})$$

$$V_x = 0 \Rightarrow V_+ = V_-; 100e^{-1000t} = 100(1 - e^{-1000t}), 2e^{-1000t} = e^{1000t} = 2,$$

$$t = \ln 2 \text{ msec} = 0.693 \text{ msec}$$

27. When $V_i = +1V$, $\frac{V_o}{V_i} = -2$; $V_o = -2V$, When $V_i = -1V$, $\frac{V_o}{V_i} = -4$; $V_o = 4V$

28. Characteristic equation of 'A' is $|A - \lambda I| = 0$

$$\Rightarrow \begin{vmatrix} 1-\lambda & 2 \\ -1 & 3-\lambda \end{vmatrix} = 0$$

$$\Rightarrow \lambda^2 - 4\lambda + 5 = 0$$

By Hamilton theorem $\Rightarrow A^2 - 4A + 5I = 0$

$$\Rightarrow A^2 = 4A - 5I \quad \dots\dots(1)$$

$$\Rightarrow A(A^2) = A(4A - 5I)$$

$$\Rightarrow A^3 = 4A^2 - 5A \quad \dots\dots(2)$$

$$\Rightarrow A^4 = 4A^3 - 5A^2 \quad \dots\dots(3)$$

$$\Rightarrow A^5 = 4A^4 - 5A^3 \quad \dots\dots(4)$$

$$\Rightarrow A^6 = 4A^5 - 5A^4 \quad \dots\dots(5)$$

$$\text{Now } A^6 - 4A^5 + 8A^4 - 12A^3 + 14A^2$$

$$= 4A^5 - 5A^4 - 4(4A^4 - 5A^3) + 8(4A^3 - 5A^2) - 12(4A^2 - 5A) + 14(4A - 5I)$$

$$= -4A + 5I \quad (\because \text{by applying equations (1),(2),(3),(4) \& (5)})$$

29. Full load current = $\frac{100(10^3)}{\sqrt{3} \times 440} = 131.2 \text{ A}$

Field loss = $\frac{200^2}{150} \text{ W} = 267 \text{ W}$

Armature loss = $3 \times \left(\frac{131.2}{2} \right)^2 \times 0.02$
= 258 W

Total losses = 1304.87 W

Losses = $\left(\frac{1}{\eta} - 1 \right) \text{ output}$

output = 100 kW

$1304.87 = \left(\frac{1}{\eta} - 1 \right) 100 \text{ kW}$

$\eta = 98.8\%$

or

Output = 100 kW

Input = $100 + 1304.87 = 101304.87$

$\therefore \eta = \frac{100}{101304.87} = 98.8\%$

30. L-G-fault

$I_{\text{base}} = \frac{100 \text{ MVA}}{11 \text{ K}} = 9.09 \text{ KA}$

$I_f = 3I_{R0} = \frac{3E_{R1}}{X_{1eq} + X_{2eq} + X_{0eq}}$

$= \frac{3 \times 1.0}{0.15 + 0.15 + 0.05} = \frac{3}{0.35} = 8.57 \text{ PU}$

$I_f \text{ in KA} = \text{IPU} \times I_{\text{base}} = 8.57 \times 9.09 = 78 \text{ KA}$

31. Given $f_1 = 1 \text{ MHz}$; $c_1 = 420 \text{ PF}$

$f_2 = 1.5 \text{ MHz}$; $c_2 = 140 \text{ PF}$

$c_d = \frac{n^2 c_2 - c_1}{1 - n^2}$; $n = \frac{f_2}{f_1} = \frac{1.5}{1} = 1.5$

$\Rightarrow c_d = \frac{420 \times 2.25 - 140}{2.25 - 1} = 84 \text{ PF}$

32.

$$\text{The turn on loss} = \frac{1}{6} \times v_{dc} \times I_o \times T_{on}$$

$$\therefore \text{Turn on energy loss} = \frac{1}{6} \times v_{dc} \times I_o \times T_{on}$$

$$\text{Turnoff energy loss} = \frac{1}{6} \times v_{dc} \times I_o \times T_{off}$$

$$\therefore \text{Switching loss} = \frac{1}{6} \times 100 \times 20 \times 0.1 \times 10^{-6} + \frac{1}{6} \times 100 \times 20 \times 0.1 \times 10^{-6} = 66.67 \times 10^{-6} \text{ J}$$

$$\text{conduction energy loss} = v_o \times I_o + I_o^2 \times R_d \times 0.1 \times 10^{-3}$$

$$= [1 \times 20 + (20)^2 \times R_d] \times 10^{-4}$$

$$\therefore \text{Average power loss} = \frac{(66.67 \times 10^{-6} + [20 + 400R_d] \times 10^{-4})}{0.2 \times 10^{-3}} = \frac{\Delta T}{\theta_{JC}}$$

$$\Rightarrow 66.674 \times 10^{-6} + 20 \times 10^{-4} + 400R_d \times 10^{-4} = 100 \times 0.2 \times 10^{-3} \Rightarrow R_d = 0.448 \Omega$$

33. Ohmic loss at $\frac{5}{4}$ loading is 100 W, so ohmic-loss at rated condition (S.C. loss)

$$P_{sc} = 100 \times \left(\frac{4}{5}\right)^2 = 64 \text{ W}.$$

Let maximum efficiency occurs at 'x' loading.

For maximum efficiency

Variable loss = fixed loss

ohmic loss = core-loss

$$\Rightarrow x^2 \cdot 64 = 50$$

$$x = 0.88$$

$$\text{So, } \eta_{\max} = \frac{20 \times 1 \times 0.88}{20 \times 1 \times 0.88 + 0.05 + 0.064 \times 0.88^2} = 0.994 = 99.4\%$$

34. Given $\cos \phi = 0.3 \Rightarrow \phi = 1.266$

$$R_p = 2500 \Omega; L = 20 \text{ mH}; V = 120 \text{ V}; I = 10 \text{ A}$$

$$\text{Power consumed by load, } P_T = VI \cos \phi = 120 \times 10 \times 0.3 = 360 \text{ W}$$

$$\beta = \tan^{-1} \left(\frac{X_L}{R_p} \right) = \tan^{-1} \left(\frac{2\pi fL}{R_p} \right) = \tan^{-1} \left(\frac{2\pi \times 50 \times 20 \times 10^{-3}}{2500} \right) = 0.00251 \text{ rad}$$

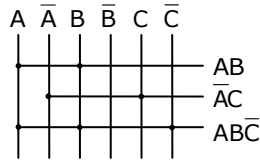
$$\begin{aligned} \text{Actual wattmeter reading} &= [1 + \tan \phi \tan \beta] \text{ true power} \\ &= [1 + \tan 72.54^\circ \tan 0.143^\circ] 360 = 362.87 \text{ W} \end{aligned}$$

$$\text{Power loss, } P_L = \frac{V^2}{R_p} = \frac{120^2}{2500} = 5.76 \text{ W}$$

$$\text{Total wattmeter reading} = 362.84 + 5.76 = 368.63 \text{ W}$$

$$\therefore \% \text{ Error} = \frac{P_w - P_T}{P_T} \times 100 = \frac{368.63 - 360}{360} \times 100 = 2.397\%$$

35.



	Q_A	Q_B	Q_C	Q_D
1 {	0	0	0	0
2 {	1	0	0	0
3 {	1	1	0	0
4 {	0	1	1	0
5 {	0	0	1	1
6 {	0	0	0	1
	0	0	0	0

36. (A) Given $P(A) = \frac{20}{100} = \frac{1}{5}$, $P(B) = \frac{30}{100} = \frac{3}{10}$, $P(C) = \frac{50}{100} = \frac{1}{2}$

Let 'D' denote that the bolt is defective

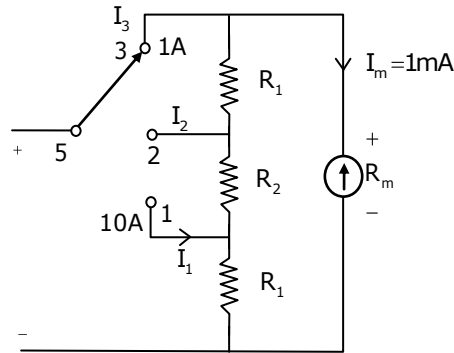
Given $P(D / A) = \frac{6}{100} = \frac{3}{50}$, $P(D / B) = \frac{3}{100}$, $P(D / C) = \frac{2}{100} = \frac{1}{50}$

\therefore By Bayes's theorem $P(C / D) = \frac{P(C)P(D / C)}{P(A)P(D / A) + P(B).P(D / B) + P(C)P(D / C)}$

$$= \frac{\frac{1}{2} \cdot \frac{1}{50}}{\frac{1}{5} \cdot \frac{3}{50} + \frac{3}{10} \cdot \frac{3}{100} + \frac{1}{2} \cdot \frac{1}{50}} = \frac{10}{31}$$

37. $A_v = \frac{-h_{fe}R_c}{h_{ie} + 1 + h_{fe} R_e} = -20$

38.



In position 1, R_1 is in shunt with $R_2 + R_3 + R_m$

$$\therefore I_1 R_1 = I_m R_2 + R_2 + R_3$$

Given $I_1 = 10A$

$$I_m = 1mA$$

$$R_m = 50\Omega$$

$$\therefore 10R_1 = 1 \times 10^{-3} [R_2 + R_3 + 50] \Rightarrow R_1 = 10^{-4} [R_2 + R_3 + 50]$$

In position 2, $R_1 + R_2$ is in shunt with $R_3 + R_m$

$$I_2 R_1 + R_2 = I_m R_3 + R_m$$

↑

$$5A \quad 5 R_1 + R_2 = I_m R_3 + R_m$$

$$5 R_1 + R_2 = 1 \times 10^{-3} [R_3 + 50]$$

$$\therefore R_1 + R_2 = 1 \times 10^{-3} [R_3 + 50] \Rightarrow R_1 + R_2 = 2 \times 10^{-4} [R_3 + 50]$$

In position 3, $R_1 + R_2 + R_3$ is in shunt with R_m

$$I_3 R_1 + R_2 + R_3 = I_m R_m$$

↓

$$1A \therefore R_1 + R_2 + R_3 = 1 \times 10^{-3} \times 50 = 0.05$$

$$R_1 + R_2 + R_3 = 0.05$$

$$R_1 + R_2 = 2 \times 10^{-4} [R_3 + 50] \Rightarrow R_3 = 0.0399 \Omega$$

$$R_1 + R_2 = 0.01, \quad R_2 = 0.01 - R_1$$

$$R_1 = 10^{-4} R_2 + R_3 + 50$$

$$R_1 = 10^{-4} [0.01 - R_1 + 0.0399 + 50]$$

$$\therefore R_1 = 0.005 \Omega, \quad R_2 = 0.005 \Omega$$

39. By Stoke's theorem, we have

$$\int_C \vec{F} \cdot d\vec{r} = \int_S \text{curl } \vec{F} \cdot \vec{N} \, ds$$

$$\text{Finding curl } \vec{F} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ yz & xz & xy \end{vmatrix} = 0$$

$$\Rightarrow \int_S \text{curl } \vec{F} \cdot \vec{N} \, ds = 0 \Rightarrow \int_C \vec{F} \cdot d\vec{r} = 0$$

40. Given $c = 25\text{nF}$

When device is off

The voltage across capacitor $C = V_c = -V_s \cdot e^{-\frac{1}{RC}t} + V_s$

$$V_s = 100\text{V} \Rightarrow V_c = -100 \times e^{-\frac{1}{RC}t} + 100$$

$$\therefore \frac{dV_c}{dt} = \frac{100}{RC}$$

$$\text{Given minimum charging current } 10\text{mA} = C_J \times \left(\frac{dV_c}{dt} \right)$$

$$\Rightarrow 10 \times 10^{-3} = \frac{100}{R \times C} \times C_J = \frac{100}{R \times 25 \times 10} \times 20 \times 10^{-12}$$

$$\therefore R = 8\Omega$$

$$\therefore \text{minimum value of } R = 8\Omega$$

41. We have $\frac{dT}{dt} = -K(T - C)$ $T \rightarrow$ temperature at any time 't'

$C \rightarrow$ Room temperature

given $\frac{dT}{dt} = -15$; at $t = 0, T = 190, C = 70$

$$\Rightarrow -15 = -k(190 - 70)$$

$$\Rightarrow \boxed{k = 0.125}$$

$$\Rightarrow \frac{dT}{dt} = -0.125(T - 70); T(0) = 190 \Rightarrow dT = -0.125(T - 70)dt$$

$$\Rightarrow \int \frac{1}{T - 70} dT = \int -0.125 dt$$

$$\Rightarrow \log_e(T - 70) = -0.125t + c$$

$$\begin{aligned} \Rightarrow T - 70 &= e^{-0.125t+c} = e^{-0.125t} \cdot e^c \\ &= e^{-0.125t} \cdot a \text{ where } a = e^c \end{aligned}$$

$$\Rightarrow T = ae^{(-0.125)t} + 70$$

$$\Rightarrow T(t) = ae^{(-0.125)t} + 70$$

$$T(0) = 190$$

$$\Rightarrow T(0) = ae^0 + 70$$

$$\Rightarrow \boxed{a = 120}$$

$$\therefore T(t) = 120e^{-0.125t} + 70 \dots (1)$$

given $T(t) = 143^\circ\text{F} \Rightarrow t = ?$

from (1), $t = 3.98 \text{ min}$

42. For unit step input, Laplace Transform is $\frac{1}{s}$.

Taking iv option, $L[F t] = -\frac{0.1}{s} \cdot \frac{1}{s} = \frac{-0.1}{s^2}$

Taking iii option, $L[f t] = \frac{-5}{-20s+1} \cdot \frac{1}{s}$, $y = \frac{-5}{-20} \left[\frac{1}{s - \frac{1}{20}} \cdot \frac{1}{s} \right] = 5 e^{t/20} - 1$

43. $t_c = \frac{CV_s}{I_0} = \frac{2 \times 10^{-6} \times 200}{10} = 40 \mu\text{s}$

44. Internal voltage drop $= ZI = \frac{1200}{200} \times 50 = 300 \text{ V}$

46. $h[n] = e^{2n}u[n-1]$

For stability

$$\sum_{n=-\infty}^{\infty} |h[n]| < \infty$$

$$\sum_{n=-\infty}^{\infty} e^{2n}u[n-1] = \sum_{n=1}^{\infty} e^{2n} = \sum_{n=1}^{\infty} e^{2 \cdot 4}$$

$\therefore e^2 > 1 \rightarrow$ as $n \rightarrow \infty$, summation tends to ∞ hence $h[n]$ is unstable.

For causal

$h[n] = 0$ For $n < 0$

$$e^{2n}u[n-1] = \begin{cases} e^{2n} & n \geq 1 \\ 0 & n < 1 \end{cases}$$

\therefore Hence it is causal

For Memory system

Any system o/p depends upon present i/p and past o/p and the past i/p then that system is

memory system

$$\therefore h[3] = e^6u[2]$$

\therefore It is memory system

47. Given $E_o = 5V$, $E_{dc(max)} = 13.5$, $E_{dc(min)} = 10V$, $I_o = 10A$, $\Delta I = 500$ mA

From Equation, $\left(\alpha = \frac{E_o}{E_{dc}} \right) \therefore \frac{T_{on}}{T} = \frac{E_o}{E_{dc}}$

$$\therefore T_{on(max)} = \frac{E_o}{E_{dc(min)} f} = \frac{5}{10 \times 50 \times 10^3} = 10 \mu\text{sec}$$

\therefore Maximum period of conduction for switch = $10 \mu\text{sec}$

48. KCL across Loop 1, $\frac{10-V_1}{20} = i_1 + \frac{V_1}{20}$

$$V_2 - V_1 = 1 \quad \text{and} \quad V_2 = 10i_1$$

$$\therefore V_1 = 2V$$

$$49. \quad \frac{10 - V_{th}}{20} = i_1$$

$$10i_1 - V_{th} = 1$$

$$i_1 = \frac{V_{th} + 1}{10}$$

$$\frac{10 - V_{th}}{20} = \frac{V_{th} + 1}{10}$$

$$10 - V_{th} = 2V_{th} + 2$$

$$3V_{th} = 8$$

$$V_{th} = \frac{8}{3} = 2.666$$

$$50 \& 51. \quad Z_1 = 200 \Omega \quad Z_2 = 500 \Omega$$

$$Z_3 = 1000 \Omega \quad V_f = 2000 \text{ V}$$

$$i_f + i_r = i_1 + i_2$$

$$\frac{V_f}{Z_1} - \frac{V_r}{Z_1} = \frac{V_t}{Z_2} + \frac{V_t}{Z_3}$$

$$V_f - V_r = V_t \left[\frac{1}{Z_2} + \frac{1}{Z_3} \right] \quad Z_1 = V_t \left[\frac{1}{500} + \frac{1}{1000} \right] 200$$

$$= V_t \left[\frac{3}{1000} \right] \times 200 = \left(\frac{3}{5} \right) V_t$$

$$\text{Also } V_f + V_r = V_t \Rightarrow V_f - V_r = \frac{3}{5} V_t$$

$$\text{Add } 2V_f = \frac{8}{5} V_t \Rightarrow V_f = \frac{4}{5} V_t$$

$$2000 = \frac{4}{5} V_t \quad V_f = 2000 \text{ V}$$

$$V_t = 2500 \text{ V}$$

$$\text{Reflected voltage} = V_r = V_t - V_f = 2500 - 2000 = 500 \text{ V}$$

$$\text{Current transmitted in the } 500 \Omega \text{ line, } i_1 = \frac{V_t}{Z_2} = \frac{2500}{500} = 5 \text{ A}$$

$$\text{Current transmitted in the } 1000 \Omega \text{ line, } i_2 = \frac{V_t}{Z_3} = \frac{2500}{1000} = 2.5 \text{ A}$$

$$\text{Current in cable} = i_1 + i_2 = 5 + 2.5 = 7.5 \text{ A}$$

52. $x_1 = x_2 = 3r_1 = 3r_2$

$$T_e = \left(\frac{3V^2}{Cv_s} \right) \left[\frac{1}{\left(r_1 + \frac{r_2}{s} \right)^2 + x_1 + x_2^2} \right] \left(\frac{r_2}{s} \right)$$

$$425 = \left(\frac{3V^2}{Cv_s} \right) \left[\frac{1}{\left(\left[\frac{1}{0.04} \right]^2 + (3+3) \right) r_2} \right] \left[\frac{r_2}{0.04} \right]$$

$$425 = \left(\frac{3V^2}{w_s} \right) \frac{1}{28.48}$$

$$\boxed{\frac{3V^2}{Cv_s} = 12104}$$

$$\text{Test} = \left(\frac{3V^2}{Cv_s} \right) \left[\frac{1}{\left[(1+1)^2 + (3+3)^2 \right] r_2} \right] \left(\frac{t_2}{1} \right)$$

$$= (12104) \left(\frac{1}{40} \right) = 302.6 \text{ N-m}$$

53.

$$SmT = \frac{r_2}{\sqrt{r_1^2 + (x_1 + x_2)^2}} = \frac{1}{\sqrt{1^2 + (3+3)^2}} = 0.1643$$

$$Tem = \left(\frac{3V^2}{Cv_s} \right) \left[\frac{1}{\left(\left(1 + \frac{1}{0.1643} \right)^3 + (3+3)^2 \right) r_2} \right] \times \left(\frac{r_2}{0.1643} \right)$$

$$= (12104) \frac{1}{14.16} = 854.8 \text{ Nm}$$

$$\frac{\text{Test}}{\text{Tem}} = \frac{302.6}{854.8} = 0.354$$

54. $x(t) = 4 + 3e^{j2\pi t} + 3e^{-j2\pi t} + 5e^{j6\pi t} + 5e^{-j6\pi t}$

$$x(t) = 4 + 6 \cos 2\pi t + 10 \cos 6\pi t$$

$$g(t) = 8 + 6 \cos 2\pi t$$

55. DC value of y_t

$$y_t = H_w \text{ DC value of } g_t$$

$$H_w = \frac{1}{1 + j2\pi fRC}$$

$$RC = 1$$

$$\omega = 0$$

$$H_0 = 1$$

$$Y_t|_{DC} = 8$$

60. S.I for 1 year = Rs. (900 – 800) = Rs.100

S.I for 4 years = Rs. (100 × 4) = Rs.400

Principal = Rs.400

62. Suppose X will cost 40 paisa more than Y after 2 years, then

$$4.20 + 0.40Z - 6.30 + 0.15Z = 0.40$$

$$0.25Z = 0.40 + 2.10 \Rightarrow Z = 10$$

$$\text{Required year} = 2001 + 10 = 2011$$

63. C's 1 day of work = $\frac{1}{3} - \left(\frac{1}{6} + \frac{1}{8}\right) = \frac{1}{24}$

$$A's \text{ wages} : B's \text{ wages} : C's \text{ wages} = \frac{1}{6} : \frac{1}{8} : \frac{1}{24} = 4 : 3 : 1$$

$$C's \text{ share for 3 days} = 3 \times \frac{1}{24} \times 3200 = \text{Rs.400}$$

64. Let the three integers be $x, x + 2, x + 4$

$$3x = 2x + 4 + 3 \Rightarrow x = 11$$

$$\text{Third integer} = 11 + 4 = 15$$

65. From the data it is not given that percentage of proteins in skin is 16%

Rather it is given that percentage entire human body is 16%

Therefore, we should not do 16% of 1/10